

# ACCURACY OF eA MEASUREMENTS AT eRHIC

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## SYNOPSIS

- ① STUDY OF INCLUSIVE MEASUREMENTS

$$eA \rightarrow e' X$$

- TRIGGERED BY  $e'$  OR EJECTED QUARK

- ② COMPUTE COUNT RATES USING ONE PHOTON EXCHANGE APPROXIMATION:-

$$\frac{d^2\sigma}{dx dQ^2} = \frac{4\pi\alpha^2}{x Q^4} \left[ 1 - y + \frac{y^2}{2(1+R)} \right] F_2(x, Q^2)$$

$$F_2 = \sum e_i^2 \times g_i(x, Q^2)$$

$g_i(x, Q^2) + R(x, Q^2)$  COMPUTED FROM MRSA.

- ③ COMPUTE STATISTICAL ACCURACIES

- SYSTEMATIC ERRORS NEED TO BE ADDRESSED.

- ④ CONCENTRATE ON SHADOWING MEASUREMENTS

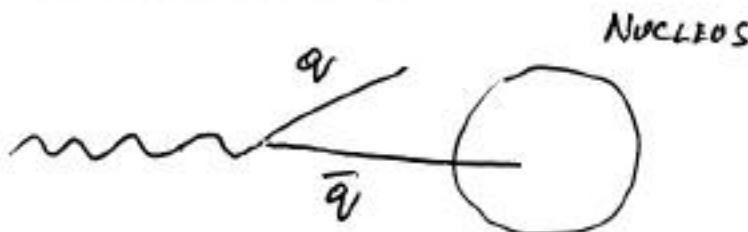
$$R_{NAC} = \frac{F_2^A}{F_2^D} \approx \frac{\text{COUNT RATE FROM } A}{\text{--- } " \text{ --- } D} [R?]$$

# WHY SHADOWING?

(2)

## MODELS

### - LAB FRAME ARGUMENT.



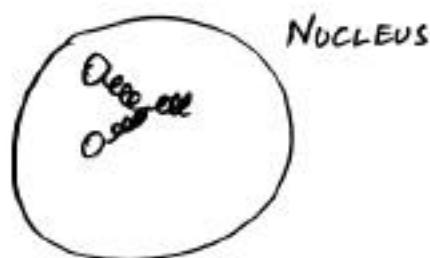
SCHILDNER  
SHAW  
BRODSKY, HOYER  
HELMICH, TOME  
PILLER, RITZEN  
WEISE

(9)

DOUBLE SCATTER AMPLITUDE INTERFERES  
DESTRUCTIVELY WITH SINGLE SCATTER  
SINCE AMPLITUDES ARE IMAGINARY.

$$\therefore \sigma_{\gamma A} < A \sigma_{\gamma N}$$

### - LIGHT CONE ARGUMENT



NICHOLAEV, ZAKHAROV  
MUELLER, QIU.

- DENSE SOFT PARTONS FROM ONE NUCLEON  
FUSE TO DEPLET E PARTONS AT VERY LOW  $x$ .  
( $x \lesssim 0.01$ )

- LEADS TO ACCRETION OF MOMENTUM  
AT HIGHER  $x$  ( $\sim 0.05$ ) i.e. ANTI SHADOWING

CAN SHADOWING LIMIT GROWTH OF  $F_2 \rightarrow Q^2$  (3)  
AT SMALL  $x$ ?

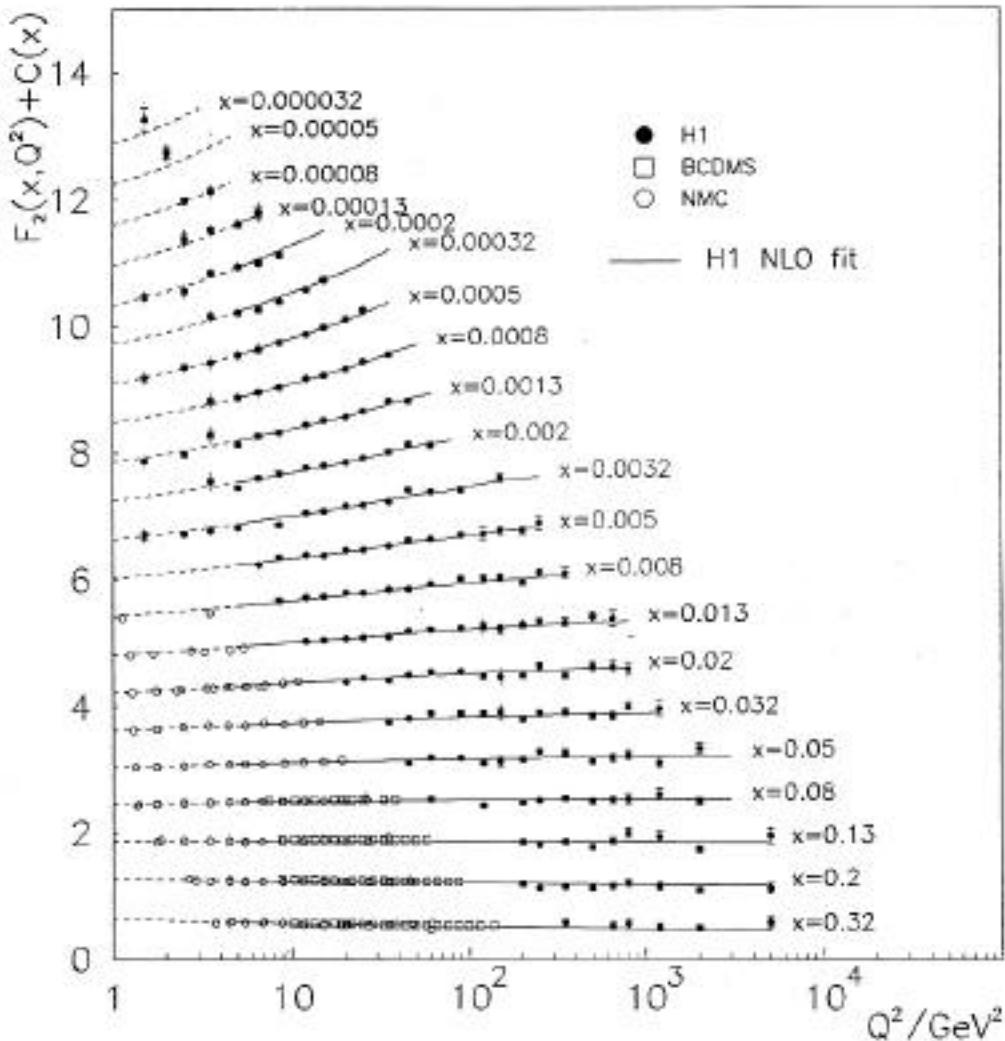


Figure 11:  $F_2(x, Q^2)$  measured by H1 together with BCDMS [41] and NMC [40] fixed target results. The full line corresponds to the NLO QCD fit, see sect. 7.4, which includes the data for  $Q^2 \geq 5 \text{ GeV}^2$ . The extension of the curves below  $5 \text{ GeV}^2$  represents only the backward evolution of the fit. The  $F_2$  values are plotted in a linear scale adding a constant  $c(x) = 0.6(i - 0.4)$  where  $i$  is the  $x$  bin number starting at  $i = 1$  from  $x = 0.32$ . The inner error bar is the statistical error, the outer corresponds to the full error resulting from adding the statistical and systematic error in quadrature. Some H1 data points at lower  $Q^2$  were shifted to nearby  $x$  values for graphical representation of the data.

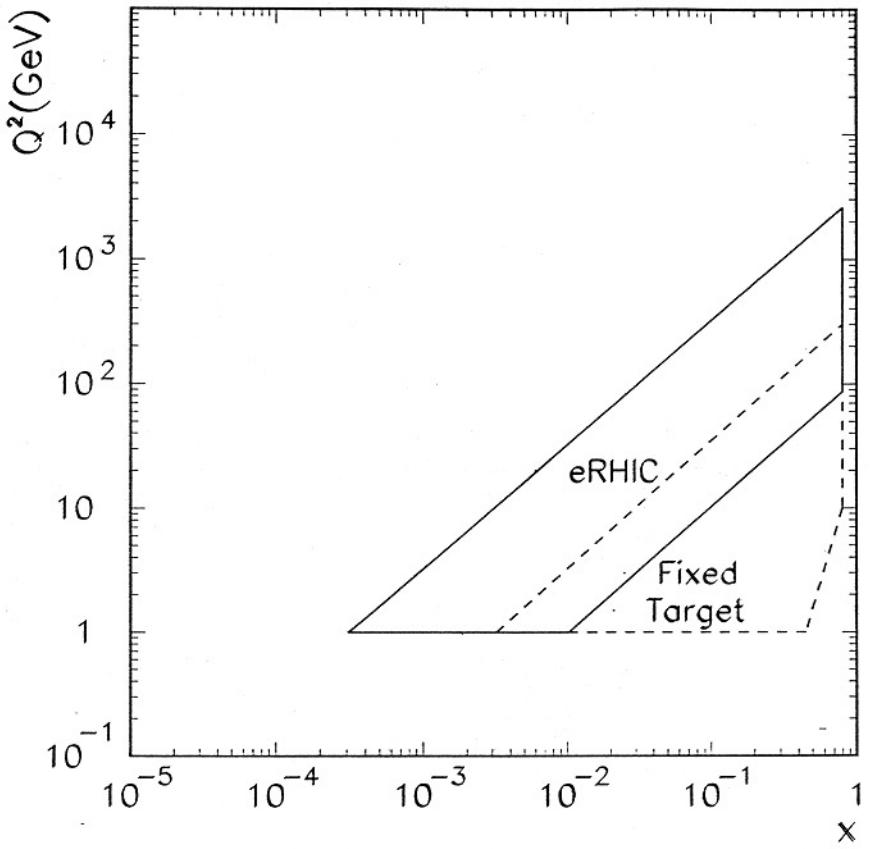


Fig 1a Kinematic ranges of the existing fixed target data compared to the projected measurements at RHIC.

$$Q^2 = S \times y \quad (.03 < y < 0.9)$$

$$y = \frac{1 - E'(1 - \cos\theta)}{2E} \approx \frac{E - E'}{E}$$

CUTS

$E' > 2 \text{ GeV}$   
 $\theta_e > 3^\circ$

OR

$E_q > 5 \text{ GeV}$   
 $\theta_q > 10^\circ$

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$$Q^2 > 1 \text{ GeV}^2$$

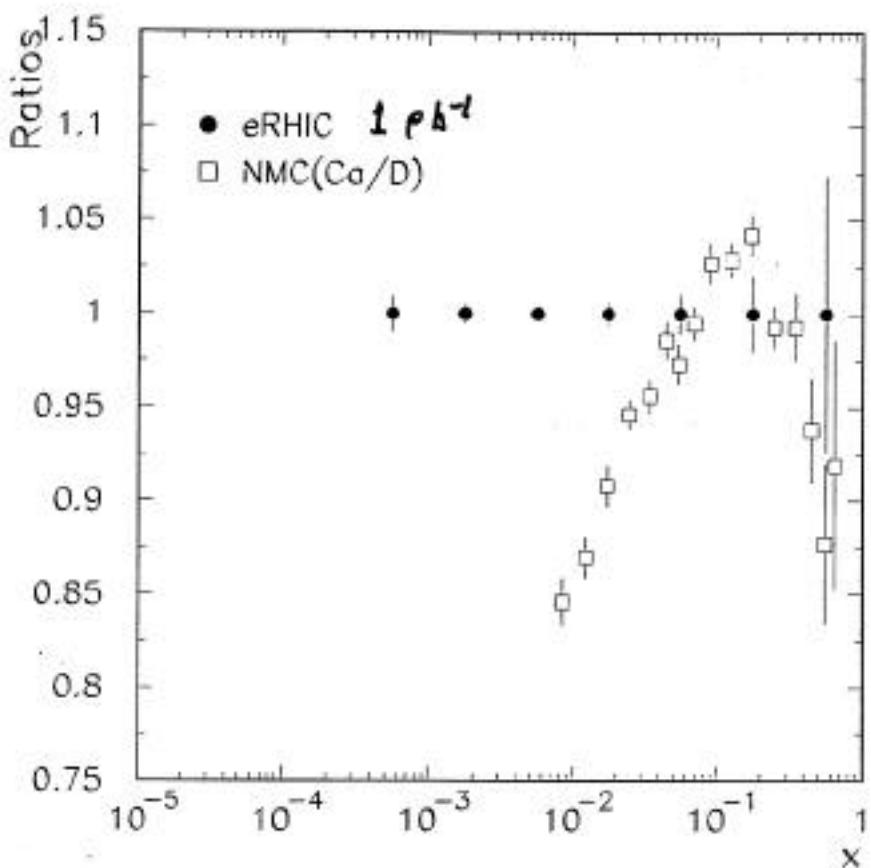


Figure 2a. The estimated accuracy per  $\text{pb}^{-1}$  luminosity of the ratios  $R_{\text{nuc}}$  at RHIC compared with the NMC measurements for Ca/D with  $Q^2 > 1 \text{ GeV}^2$ .

INTEGRATED LUMI PER YEAR ( $\sim 10^7$  Secs)

$$= \frac{10^7}{\text{sec/yr}} \times 2 \times 10^{30} \text{ pb}^{-1} \text{s}^{-1} \times 197 \times \text{fraction live}_{\text{Gold}}$$

$$= 4000 \text{ pb}^{-1}/\text{year} \times \text{fraction live}$$

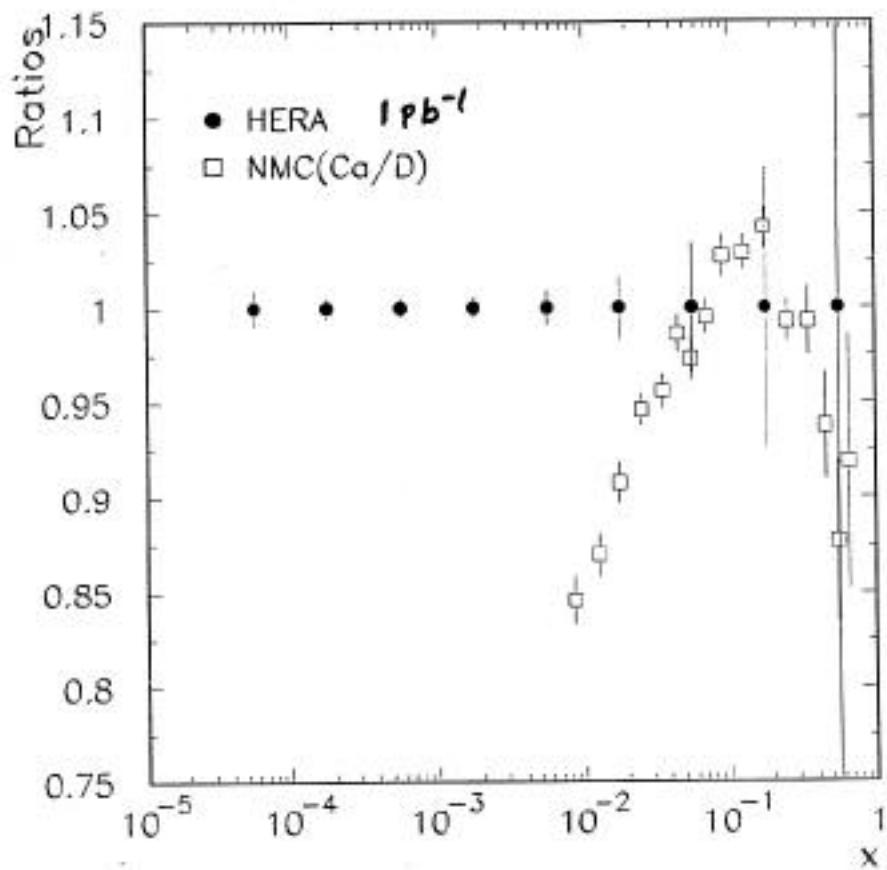


Figure 2b The estimated accuracy of the ratios  $R_{nuc}$  per  $\text{pb}^{-1}$  luminosity at HERA compared with the NMC measurements for Ca/D with  $Q^2 > 1 \text{ GeV}^2$ .

SAME CALCULATION FOR HERA PROTONS (NOW)

$$\text{INTEGRATED LUMI} = \frac{10^7}{\text{s/yr}} \times \frac{10^{31}}{\text{pb}^{-1}\text{s}^{-1}} \times \text{fraction live.}$$

$$= 100 \text{ pb}^{-1} \text{ yr}^{-1} \times \text{fraction live}$$

( $x \sim 5$ , UPGRADE)

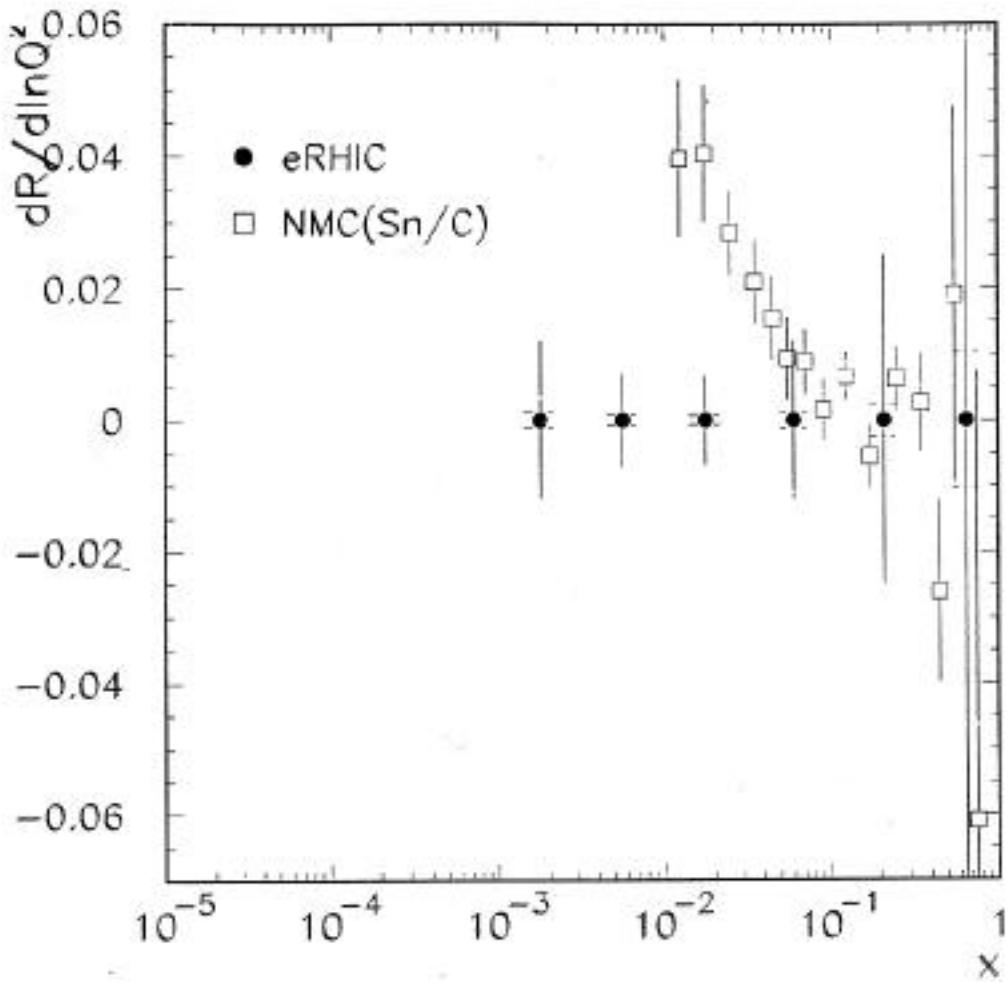


Figure 3a. The slopes  $\frac{dR}{d\ln Q^2}$  as function of  $x$  showing the NMC data [1] (open squares) and the statistical accuracy of an experiment with  $1 \text{ pb}^{-1}$  per nucleon per target at eRHIC. The inner error bars show the accuracy for an experimental luminosity of  $100 \text{ pb}^{-1}$  (ie roughly a 5 day run at eRHIC). The NMC systematic errors which are about the same size as the statistical errors are not included.

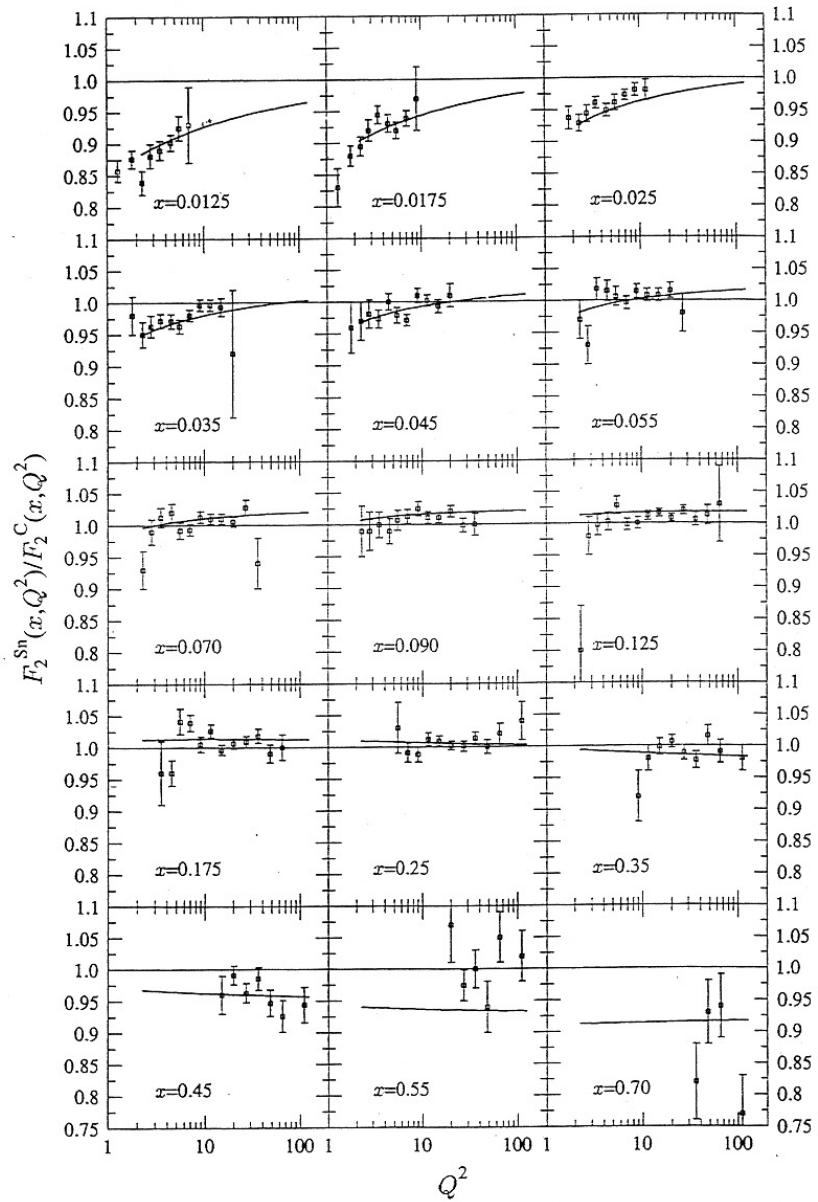


Fig. 10. The calculated scale evolution of  $F_2^{\text{Sn}}(x, Q^2)/F_2^{\text{C}}(x, Q^2)$  compared with the NMC data [3] at different fixed values of  $x$ . The data are plotted with statistical errors only.

the data. The changes in the sign of  $\partial(F_2^{\text{Sn}}/F_2^{\text{C}})/\partial Q^2$  do not seem to be in contradiction with the data either. It is also interesting to notice that

$$\int_{x_1}^{x_2} \left[ \frac{F_2^A}{F_2^D} - 1 \right] F_2^D dx = \text{CHANGE IN FRACTION OF MOMENTUM OF NUCLEON CARRIED BY QUARKS.}$$

(x <sub>CORES</sub> ~1)

(17)

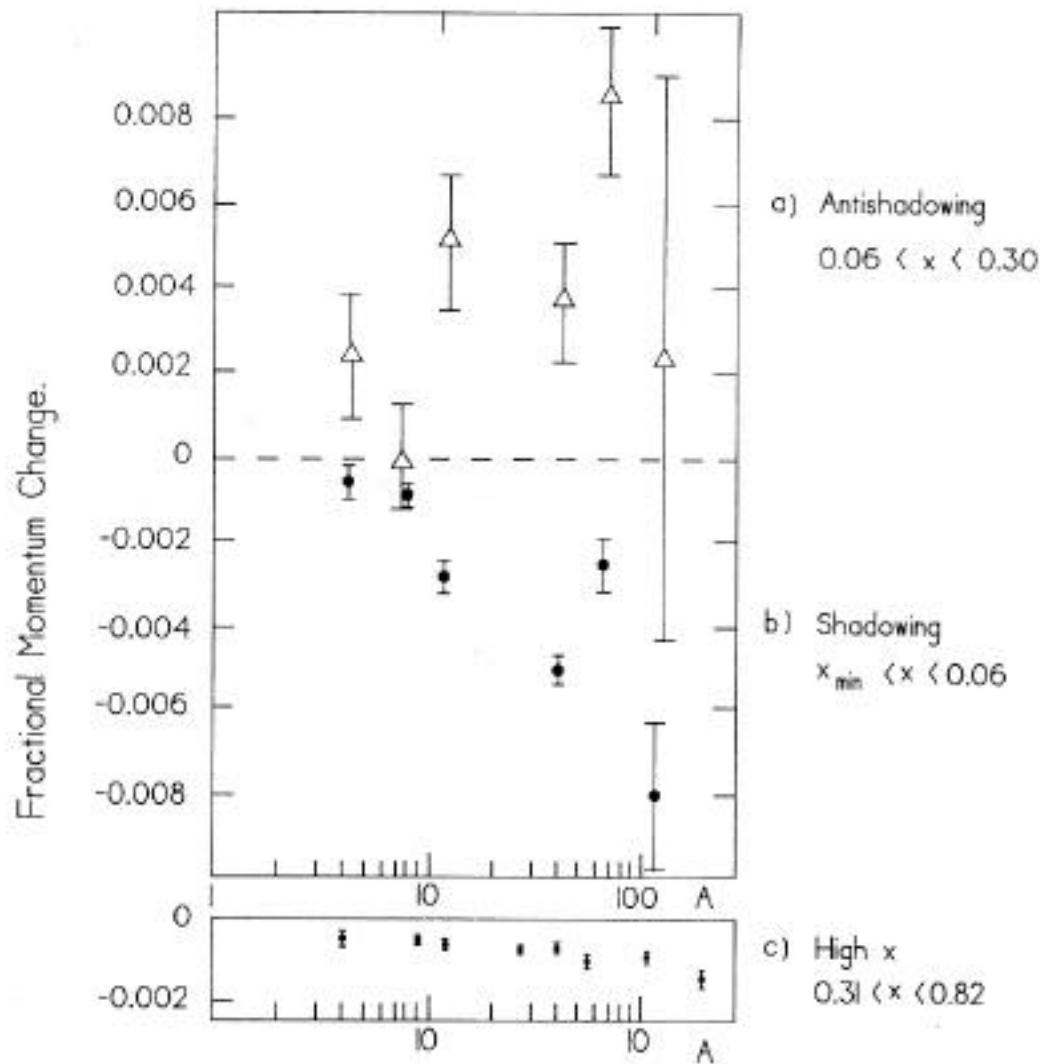


Fig. 8

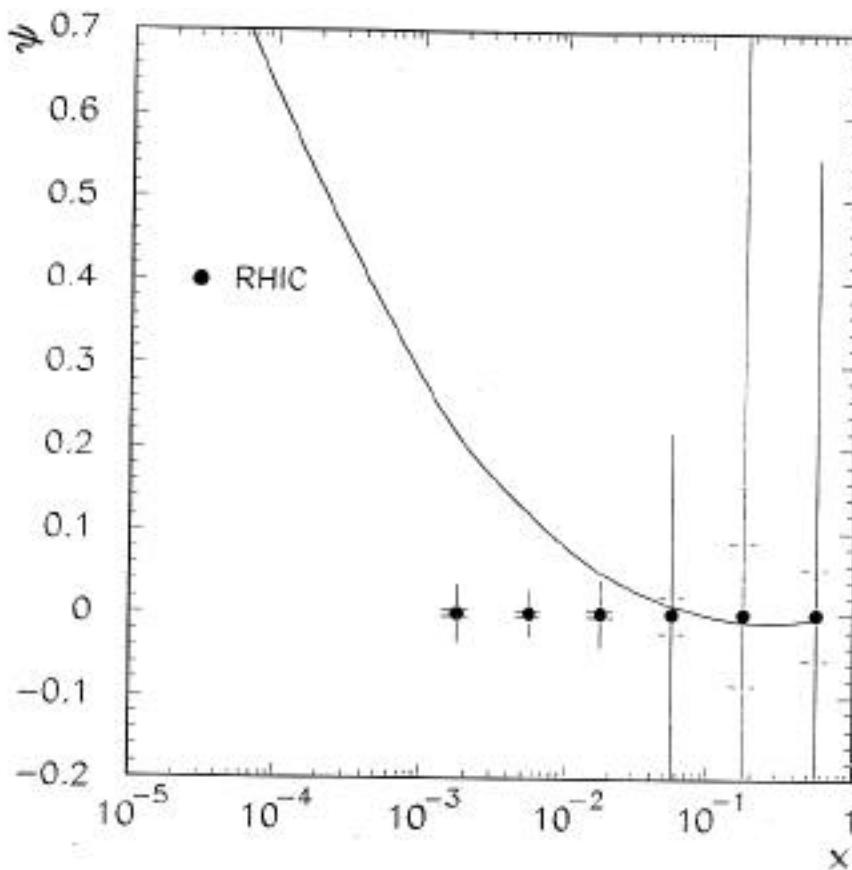


Figure 4a. The slopes  $\psi$  (see text) as a function of  $x$  showing the statistical accuracy of an experiment with  $1 \text{ pb}^{-1}$  per nucleon per target at RHIC. The smooth curve shows  $dF_2^g/d\ln Q^2$  expected from QCD and calculated from the MRSA parton distribution functions. The inner error bars show the accuracy for an experimental luminosity of  $100 \text{ pb}^{-1}$  (ie roughly a 5 day run at eRHIC).

$$\psi = \frac{\frac{dF_2^A}{d\ln Q^2} - \frac{dF_2^D}{d\ln Q^2}}{\frac{dF_2^P}{d\ln Q^2}} \approx \frac{DG}{G}$$

## EXPERIMENTAL CONSIDERATIONS

L12

- LOW ELECTRON ENERGY - 10 GeV
  - NEED TO DETECT <sup>+ IDENTIFY</sup> SCATTERED ELECTRONS DOWN TO  $E' \sim 2-3$  GeV.
- eA RHIC IS A HIGH LUMINOSITY MACHINE
  - NEED SELECTIVE TRIGGERS TO AVOID DEAD TIME PROBLEMS.
- NEED LOW A AND HIGH A NUCLEI AS WELL AS DEUTERONS
  - CAN A AND D BE STORED SIMULTANEOUSLY TO MINIMIZE SYSTEMATIC ERRORS
- NEED HERMETIC DETECTOR FOR EVENT RECONSTRUCTION
  - PROBABLY DIFFERENT FROM EXISTING RHIC DETECTORS.

## CONCLUSIONS

- VERY HIGH STATISTICAL PRECISION IS POSSIBLE AT THE HIGH LUMINOSITY eRHIC
- SYSTEMATIC ERRORS NEED TO BE CONTROLLED.